

Energy Transport State Resolved Raman for Probing Interface Energy Transport and Hot Carrier Diffusion in Few-Layered MoS

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3 **Energy Transport State Resolved Raman for Probing Interface Energy Transport and Hot**
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6 **Carrier Diffusion in Few-Layered MoS₂**
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30 **Abstract**
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34 Quantitative understanding of 2D atomic layer interface thermal resistance (R) based on Raman
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36 characterization is significantly hindered by unknown sample-to-sample optical properties
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38 variation, interface-induced optical interference, off-normal laser irradiation, and large thermal-
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40 Raman calibration uncertainties. In this work, we develop a novel energy transport state resolved
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42 Raman (ET-Raman) to resolve these critical issues, and also consider the hot carrier diffusion,
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44 which is crucial but has been rarely considered during interface energy transport study. In ET-
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46 Raman, by constructing two steady heat conduction states with different laser spot sizes, we
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48 differentiate the effect of R and hot carrier diffusion coefficient (D). By constructing an extreme
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50 state of zero/negligible heat conduction using a picosecond laser, we differentiate the effect of R
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52 and material's specific heat. In the end, we precisely determine R and D without need of laser
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54 absorption and temperature rise of the 2D atomic layer. Seven MoS₂ samples (6.6~17.4 nm) on
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3 c-Si are characterized using ET-Raman. Their D is measured in the order of $1.0 \text{ cm}^2/\text{s}$, increasing
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5 against the MoS_2 thickness. This is attributed to the weaker in-plane electron-phonon interaction
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7 in thicker samples, enhanced screening of long-range disorder, and improved charge impurities
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9 mitigation. R is determined as $1.22\sim 1.87\times 10^{-7} \text{ K}\cdot\text{m}^2/\text{W}$, decreasing with the MoS_2 thickness.
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11 This is explained by the interface spacing variation due to thermal expansion mismatch between
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13 MoS_2 and Si, and increased stiffness of thicker MoS_2 . The local interface spacing is uncovered
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15 by comparing the theoretical Raman intensity and experimental data, and is correlated with the
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17 observed R variation.
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27 **Keywords:** hot carrier diffusion, interface thermal resistance, 2D atomic layer, Raman
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29 spectroscopy, picosecond laser, energy transport state design
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3 The bottleneck of most modern technologies and energy solutions has been attributed to the
4 thermal problems at the nanoscale.¹⁻² Especially, the thermal transport across interfaces can
5 significantly influence the overall performance of nanosystems, such as microelectronics,
6 photonics, and thermoelectric devices. The direct effect on device performance is that the high
7 interface thermal resistance could cause electronic functionality catastrophic failures of nano-
8 devices.³ So accurate thermal-physical characterization of the 2D interface is very important for
9 both fundamental research and industrial applications. However, the measurement of interface
10 energy coupling is very challenging and complicated because interface thermal conductance is
11 related to the characteristics of the interface properties, such as the effect of roughness, disorder,
12 dislocations, and bonding, *etc.*⁴

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15 Besides, as has been studied in 2D semiconductor materials, the electrically and optically
16 generated hot carriers can strongly contribute to the thermal diffusion and heat dissipation in
17 electronic devices.⁵ For example, when scaling down the devices, the hot carrier could also
18 induce the degradation of MOSFETs which will cause time-dependent shift in the measured
19 devices parameters.⁶ For photo-detection and photovoltaics devices, thermalization of the light-
20 induced hot carrier contributes to most of the efficiency loss.⁷ The transport of hot carriers, like
21 free electrons in metals, is dominated by various interactions between carriers and other
22 elementary excitations in semiconductor materials.⁸ Therefore, the study of hot carrier transport
23 could provide us deep insight about the scattering process and energy distribution in
24 semiconductors.

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27 To date, several approaches have been applied to study the interface thermal transport between
28 2D material and its substrate either by experiment or theoretical simulation. Some well-known
29 experiment techniques include the 3ω method,⁹ thermoreflectance method including both time-

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3 domain and frequency-domain analysis,¹⁰ and Raman based thermal probing method.¹¹⁻¹² For
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5 theoretical methods, molecular dynamics (MD) simulation¹³ and acoustic/diffuse mismatch
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7 model¹⁴ are widely used. Remarkably, for using Raman-based techniques, the hot carrier
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9 diffusion effect on thermal transport has not been carefully taken into account before. This
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11 usually leads to an underestimated heating area because the hot carrier diffusion could
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13 significantly extend the heating size. As a result, an overestimated laser heating flux could lead
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15 to less accurate thermal properties evaluation (*e.g.*, underestimated interface thermal resistance).
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17 On the other hand, for the hot carrier diffusion study, the most common and straight forward
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19 approach is to apply a voltage to the electric contact to control the electron population in the
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21 material. Unfortunately, there is still a concern that the electrical contacts may cause screening
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23 disorder in field-effect transistors.¹⁵ Thus, optical-based measurements are believed to provide
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25 the intrinsic hot carrier transport properties of the material. To this end, several optical
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27 techniques including transient grating,¹⁶ photoluminescence (including both time-of-flight
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29 configuration¹⁷ and the spatially resolved geometry¹⁸), and spatially and temporally resolved
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31 pump-probe techniques¹⁹⁻²⁰ have been used to study the hot carrier diffusion. These techniques
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33 allow us to directly observe the expansion of the carrier density profile so that any changes in the
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35 diffusion coefficient caused by carrier or lattice temperature could be studied simultaneously.
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37 However, most of these work are focused on graphene,²¹ reduced graphene oxide,²²⁻²³ CdSe,¹⁶
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39 *etc.* For the promising semiconductor materials-transition metal dichalcogenides (TMDs), less
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41 work has been reported so far.
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51 For the optical-based measurement of both interface thermal resistance (R) and carrier diffusion
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53 coefficient, the optical properties [the refractive index (n) and extinction coefficient (k_L)] of the
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55 samples are the must-know parameters. They are related to the interaction between a material
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3 and incident light and vary a lot from sample to sample. Especially, for real 2D interface
4 structure (e.g. MoS₂ nanosheets on SiO₂ substrate), a tiny change of the local spacing can
5 significantly change the laser optical absorption, leading to large measurement errors.²⁴
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8 Additionally, like the Raman-based techniques developed by Cai *et al.*²⁵ and Judek *et al.*²⁶ to
9 explore the 2D interface thermal transport properties, the laser absorption coefficient can only be
10 estimated based on others' work rather than direct measurement, which could introduce great and
11 yet unevaluated errors. The measured n and k_L values also vary a lot from different methods. For
12 example, at 532 nm wavelength, the refractive index of MoS₂ is ~ 3.05 determined by
13 spectroscopic ellipsometry²⁷ and ~ 5.2 (1.7 times larger) by a spatially resolved spectrum
14 system²⁸.
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28 In our recently published work, we have developed a new technique and systemically studied the
29 hot carrier diffusion effect on thermal transport. R and D are simultaneously determined for four
30 sub-10 nm thick virgin MoS₂ on c-Si.⁵ In this work, we make another breakthrough on the basis
31 of that technique and develop a novel and more advanced technique: energy transport state-
32 resolved Raman (ET-Raman) to study the 2D materials' thermal response under different laser
33 heating states. By this technique, we could also determine R and D but completely eliminate the
34 large errors introduced by laser absorption evaluation and Raman property temperature
35 coefficient calibration. These two factors significantly affect the measurement reported in
36 literatures and are responsible for the very large reported data deviation. Our ET-Raman is based
37 on two extreme energy transport situations: zero-transport using a picosecond (ps) laser Raman
38 and steady-state using a continuous-wave (CW) laser Raman. One of the most attractive
39 perspectives is that we do not need to know the laser absorption coefficient or the temperature
40 coefficients of the Raman properties. D and R could be determined by just comparing the Raman
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3 wavenumber shift measured from different energy transport states (in time and space domains).
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5 So this technique is believed to eliminate the errors brought in by local optical absorption
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7 evaluation, temperature coefficient calibration, and the effects from electrical contact. Therefore
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9 it provides a far more accurate understanding of interface energy coupling and hot carrier
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11 diffusion. This technique is successfully applied here to determine D and R of seven few-layered
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13 MoS₂ samples on c-Si substrate. The thickness of MoS₂ nanosheets ranges from 6.6 nm to 17.4
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15 nm in this work.
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20 21 **Results and Discussions:**

22 23 24 **Physical Model of Energy Transport State-resolved Raman (ET-Raman)**

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27 In the ET-Raman technique, we construct three distinct energy transport states in both space and
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29 time domains, and probe the materials' thermal response. Figure 1 (a) shows the physical
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31 principles of this technique. A laser with 532 nm ($E=2.33$ eV) wavelength irradiates the MoS₂
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33 sample for both laser heating and Raman probe. Because the excitation energy E is greater than
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35 the band gap of MoS₂ ($E_g=1.29\sim 1.80$ eV), the absorbed photons will excite the electrons (e) to
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37 the conduction band with holes (h) left in the valence band. This excitation results in the
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39 formation of hot electrons and holes (hot carriers) because they have higher energies compared
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41 to the Fermi Energy. Then the hot carriers will lose part of the photon energy $\Delta E=(E-E_g)$ via
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43 direct phonon emission and indirect cooling through collisions with other electrons by a rapid
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45 non-radiative process, on a time scale of 0.1 ps.²⁹ This happens so quickly that the carrier
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47 diffusion during this process will not be included in this work. The hot electrons will store the
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49 rest part of photon energy (E_g) and diffuse out of the excitation spot before recombining with
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51 holes. This diffusion will result in a significantly wider thermal source spatial redistribution in
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the sample. The excited electrons and holes move together as $e-h$ pairs in this diffusion process due to the Coulomb attraction. It typically takes nanoseconds for this diffusion process so we have to consider the diffusion effect.³⁰ Since few-layered MoS₂ has an indirect bandgap, the crystal momentum conservation could strongly restrict the radiative recombination of carriers. As a result, the excited hot electrons would release the laser energy via non-radiative recombination with holes by exciting phonons. The energy of these phonons in MoS₂ nanosheets dissipates within the sample and through the interface down to the substrate to raise the local temperature. The phonons eventually reach thermal equilibrium with the electrons.

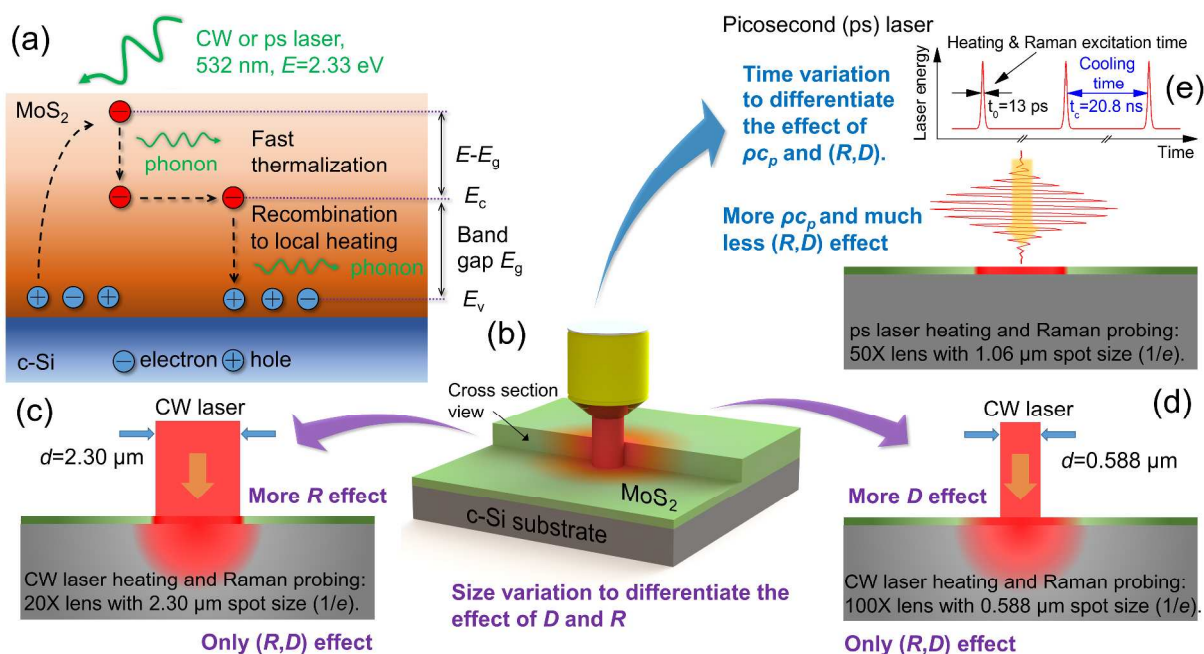


Figure 1. (a) Physical model of hot carrier generation, diffusion, and recombination in MoS₂ under laser illumination (not to scale). The photons generate hot carriers in the MoS₂ sample by exciting electrons (e) to the conduction band (E_c), leaving holes (h) in the valence band (E_v). The hot carriers transfer part of the photon energy ($E - E_g$) to the lattice in the form of thermal energy by fast thermalization (femtoseconds), diffuse out of the direct laser heating region to the low

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3 population region, and then recombine with holes to release the rest part of the photon energy (E_g)
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5 through phonon emission (carrier-phonon scattering). These hot carrier generation, diffusion, and
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7 recombination processes could strongly extend the heating area size and therefore have
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9 significant effect on the final temperature distribution. (b) An artistic illustration of the
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11 experiment concept. Examined MoS₂ nanosheets (6.6~17.4 nm thick) are placed onto the typical
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13 c-Si substrate, and a 532 nm continuous-wave (CW) laser or picosecond (ps) laser is
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15 simultaneously causing and probing the local temperature rise to generate three different energy
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17 transport states in space and time domains [(c)- (e)]. We use two objective lenses (20× and 100×)
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19 for CW laser to achieve different laser spot size heating with simultaneous Raman probing to
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21 detect the local temperature rise to study (R, D) effect. (c) Heating effect of CW laser under 20×
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23 objective. The diameter of the laser spot size is around 2.28 μm ($1/e$ profile). (d) Under 100×
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25 objective, the diameter is smaller which is around 0.588 μm ($1/e$ profile). (e) By using a ps laser,
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27 hot carriers do not have enough time to recombine with holes within every pulse width (13 ps).
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29 Also there is extremely small heat conduction from the heating region. As a result, the
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31 temperature rise is determined by the sample's volumetric heat capacity (ρc_p) with negligible
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33 effect from (R, D).
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42 The first energy transport state in our technique is the steady-state heating, and it has two sub-
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44 states with different laser heating sizes. As shown in Figure 1 (c) and (d), we use a CW laser
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46 source to generate steady-state heating to study the temperature profile that depends on (R, D)
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48 effect. Moreover, by using different objectives (20× and 100×) to have the size variation, we
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50 could differentiate the effect of D and R . In Fig. 1 (c), the laser heating spot under a 20×
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52 (NA=0.4) objective has a diameter around 2.30 μm ($1/e$ peak value). Since the MoS₂ nanosheets
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54 will absorb the laser energy, they will conduct the absorbed energy directly to substrate via R and
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3 to the in-plane direction then to the substrate via the interface (effects of both R and D). At the
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5 same time of laser heating, the same laser beam also excites Raman signal by which we could
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7 collect to get the temperature profile of the sample. By using different laser powers (P), we can
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9 obtain one parameter, called Raman shift power coefficient (RSC): $\chi_{\text{CW1}} = \partial\omega / \partial P$. As expected,
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11 χ_{CW1} is determined by R , D , laser absorption coefficient, and temperature coefficient of Raman
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13 shift. Then, as shown in Fig. 1(d), we reduce the laser heating dimension to a much smaller level
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15 by a 100 \times (NA=0.8) objective (0.588 μm), and we also obtain RSC from this experiment as χ_{CW2} .
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17 At this steady state, the D of the 2D material will have more influence on the measured
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19 temperature than that under 20 \times objective. Therefore, these two steady states construction could
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21 differentiate the effect of D and R in the measured RSC by Raman spectroscopy. Note although
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23 we mention temperature here as they are reflected in RSC, we do not need to determine the
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25 absolute temperature rise in the whole technique.
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33 The second energy transport state is completely opposite to the steady-state: it has zero-transport.
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35 In this experiment, we apply a ps laser under 50 \times (NA=0.5) objective with r_0 as 0.531 μm ($1/e$
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37 peak value) with the same wavelength as the CW laser to focus on the sample to do localized
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39 heating and Raman experiment. In the same way, we obtain the RSC for this ps laser heating
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41 case: $\chi_{\text{ps}} = \partial\omega / \partial P$. Here, we neglect the heat conduction from the heating region. Also the sample
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43 will be fully cooled to the ambient temperature during the pulse interval (see Supporting
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45 Information S1 for details). As a result, the RSC (χ_{ps}) is mainly coming from the volumetric heat
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47 capacity of the sample (ρc_p). D and R have an extremely limited contribution to the temperature
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49 rise so that we could use this heating state to distinguish the roles of ρc_p and (R , D).
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55 In our Raman experiment, the measured RSC of both MoS₂ and c-Si are Raman-intensity
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57 weighted average of the sample. For the zero-transport state, the measured temperature rise is
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also time averaged over the pulse width. Besides, we do not consider the heat loss to the environment during the Raman measurement in atmospheric condition (see Supporting Information S4 for details). All of these will be also considered in the following 3D numerical simulation for data processing.

After these three energy transport states experiments, we will define the dimensionless normalized RSC as: $\Theta_1 = \chi_{CW1}/\chi_{ps}$ and $\Theta_2 = \chi_{CW2}/\chi_{ps}$. Although χ_{CW1} , χ_{CW2} , and χ_{ps} are all influenced by the Raman temperature coefficient and the laser absorption in the sample, this normalized RSC completely rules out the effect of laser absorption and Raman temperature coefficients. Θ_1 and Θ_2 are only a function of the 2D and substrate materials' ρc_p , R , and D . Using a 3D heat conduction model to include all these properties, we could finally determine D and R of the 2D material. The whole measurement does not involve absorbed laser heating power determination and absolute temperature rise determination. This eliminates the large uncertainties brought in by these two key factors in the past measurements.

Physical model and governing equations for data processing

For the steady-state heating, the generation and diffusion of heat and electrical carriers in the sample are governed by two partial differential equations in steady state ($\partial N / \partial t = 0$).³¹⁻³² The first one is the carrier diffusion equation to determine the carrier concentration $\Delta N(r, t)$ (cm^{-3}):

$$D\nabla^2 \Delta N - \frac{\Delta N}{\tau} + \frac{\partial n_0}{\partial T_{CW}} \frac{\Delta T_{CW}}{\tau} + \Phi \alpha = 0, \quad (1)$$

where D (cm^2/s), τ (s) and Φ (photons/ cm^3s) are the carrier diffusion coefficient, the electron-hole recombination time of MoS_2 and the incident photon flux of the laser source. α (cm^{-1}) is the

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3 optical absorption coefficient of the MoS₂ nanosheets. n_0 (cm⁻³) is the equilibrium free-carrier
4 density at temperature T . The first term on the left side is related to hot carrier diffusion. The
5 second term: $\Delta N/\tau$ represents the electron-hole recombination. The thermal activation term
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$(\partial n_0 / \partial T_{CW}) \Delta T_{CW} / \tau$ is related to the carrier creation due to temperature rise. It is negligible under the relatively low-temperature rise and in small free-carrier density case.^{5, 31, 33} In our experiment, for the 6.6 nm thick sample, the temperature rise under 20× objective is estimated to be only 1.3 K/mW ($\chi_{CW1}=0.26$ cm⁻¹/mW, and the Raman temperature coefficient is estimated from our previous work⁵ as 0.20 cm⁻¹/K). Besides, the free carrier density at equilibrium could be given as $n_0 = N_s \exp(-E_g / 2k_B T)$, where N_s is the number per unit volume of effectively available states. It is in the of order 10¹⁹ cm⁻³ at room temperature and increases with temperature. k_B is the Boltzmann's constant. At room temperature, $k_B T = 0.026$ eV. So $k_B T \ll E_g$ (1.38 eV) gives a very small n_0 (room temperature) to neglect the thermal activation term. The last term $\Phi\alpha$ represents the carrier photogeneration source. In our work, the MoS₂ nanosheets are very thin (sub-20 nm) compared with its lateral dimension (5 ~ 12 μm), so we will neglect the hot carrier gradient in the thickness direction. Therefore, Eq. (1) only considers the in-plane direction diffusion.

The second equation is the thermal diffusion equation which involves the free carrier density since non-radiative recombination provides a second heat source:

$$k_T \nabla^2 \Delta T_{CW} + (h\nu - E_g) \Phi \alpha + \frac{E_g \Delta N}{\tau} = 0, \quad (2)$$

where $\Delta T_{CW}(\mathbf{r}, t)$ (K), k_T (W/mK) are the temperature rise in the steady state heating, the thermal conductivity of few-layered MoS₂. And $h\nu$ (2.33 eV) is the photon energy of the laser source.

The second term of Eq. (2), $(h\nu - E_g)\Phi\alpha$, which is proportional to $(h\nu - E_g)$, represents the heat generation due to photo-generated carriers giving off the excess energy to the MoS₂ lattice. The last term $E_g\Delta N/\tau$ contains the carrier concentration and represents the heat generation through the non-radiative recombination of free carriers.

The hot electrons will diffuse in the sample until they recombine with holes to release the energy through the non-radiative recombination transition. So the real heating area will not be merely the laser irradiating area, but will be strongly affected by the hot carrier diffusion length ($L_D = \sqrt{\tau D}$). When the laser heating spot size (radius: 0.294 μm to 1.15 μm) is comparable to, or smaller than the carrier diffusion length, this effect becomes more prominent. If the laser heating spot size is sufficiently large, the hot carrier diffusion will have less or negligible effect on the heating area. For few-layered MoS₂, the hot carrier diffusion length is in the order of 0.1 μm .^{20, 34} So we could observe different heating phenomena in MoS₂ by changing the laser heating spot size. Note that we do not consider the surface recombination process due to the *p*-type Si we used in this work. Besides, because of the long diffusion length of Si (around 700 μm), the transmitted laser energy to Si only heats it by the fast thermalization process ($\Delta E = E - E_g|_{\text{c-Si}}$). Detailed discussions for this consideration could be found in our previous work.⁵

When we use the ps laser to generate the zero-transport heating state, the laser pulse (13 ps) is so short that only the fast thermalization process happens and we could neglect the heat conduction in the lattice here as discussed above. By only considering the laser absorption in MoS₂ sample and its substrate, we have

$$\rho c_p \frac{\partial \Delta T_{\text{ps}}}{\partial t} = \alpha I \left(\frac{h\nu - E_g}{h\nu} \right), \quad (3)$$

where I (W/cm^2) is the laser intensity, t is the time. $\Delta T_{\text{ps}}(r,t)$ is the temperature rise from the zero-transport state. After considering both space and time domain Gaussian distributions, and the Beer-Lambert law, the laser intensity (heat flux) is given by:

$$I(r, z, t) = \frac{I_0}{\tau_L} \exp\left[-\frac{r^2}{r_0^2}\right] \exp\left[-\ln(2)\frac{t^2}{t_0^2}\right] \exp\left[-\frac{z}{\tau_L}\right], \quad (4)$$

where I_0 (W/cm^2) is the peak laser intensity, r_0 ($0.53 \mu\text{m}$) is the laser spot radius of ps laser, t_0 (6.5 ps) is the half pulse width. $\tau_L = \lambda/4\pi k_L$ is the laser absorption depth. $\lambda=532 \text{ nm}$ (the laser wavelength), and k_L is the extinction coefficient. So we have $\tau_L(\text{MoS}_2)=38.5 \text{ nm}$, and $\tau_L(\text{c-Si})=820 \text{ nm}$. Because the thickness of MoS_2 nanosheets (6.6 nm to 17.4 nm) is smaller than its laser absorption depth, both MoS_2 and c-Si will absorb the laser energy and be heated.

As a result, the measured temperature rise of MoS_2 is actually determined by the hot carrier diffusion coefficient and the interface thermal resistance under steady-state heating and only by laser absorption rate and ρc_p under zero-transport state heating. By solving Eqs. (1)-(4), we could rule out the laser absorption term and deduce the ratio of the temperature rise ($\bar{T}_{\text{CW}}/\bar{T}_{\text{ps}}$) of two materials from two heating states. The ratio is just the normalized RSC. Then we solve Eqs. (3) and (4) to analyze the experimental results and determine the R and D value. In our work, the temperature difference between MoS_2 and c-Si is determined and used. This treatment has taken into full consideration of the temperature rise effect of the c-Si substrate.

Figure 2 shows the schematic of the Raman experiment setup. (see Materials and Methods section for more details) Figure 2(b) is the structure of our MoS_2 supported on the c-Si substrate. Figure 2(c) shows the atomic structure of the typical layered MoS_2 . The Mo atom is in the middle

for each layer and the distance between each layer is around 0.65 nm. Figure 2(d) is the typical Raman spectrum of two vibration modes of MoS₂ (E_{2g}^1 and A_{1g}) and c-Si LO phonon mode by 532 nm laser. The E_{2g}^1 mode (~ 383 cm⁻¹) is associated with in-plane opposite vibration of two sulfur atoms with respect to the molybdenum atom, whereas the A_{1g} mode (~ 408 cm⁻¹) is associated with the out-of-plane vibration of only sulfur atoms in opposite directions.³⁵

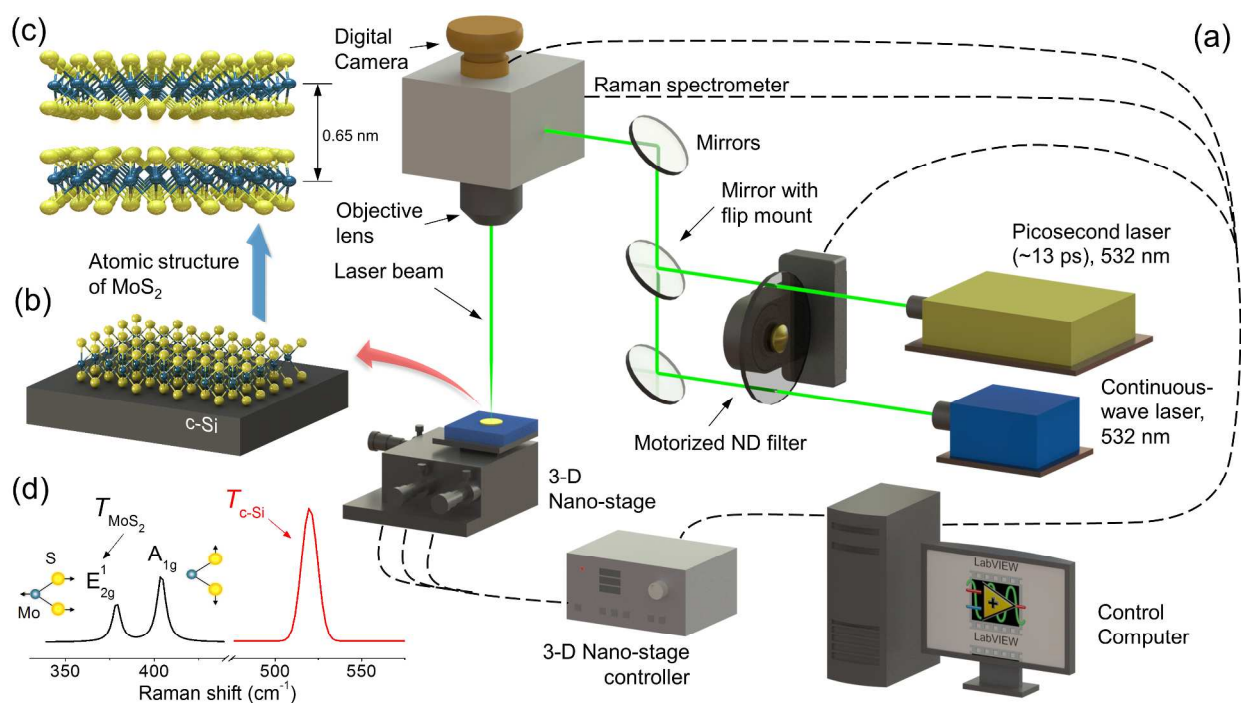
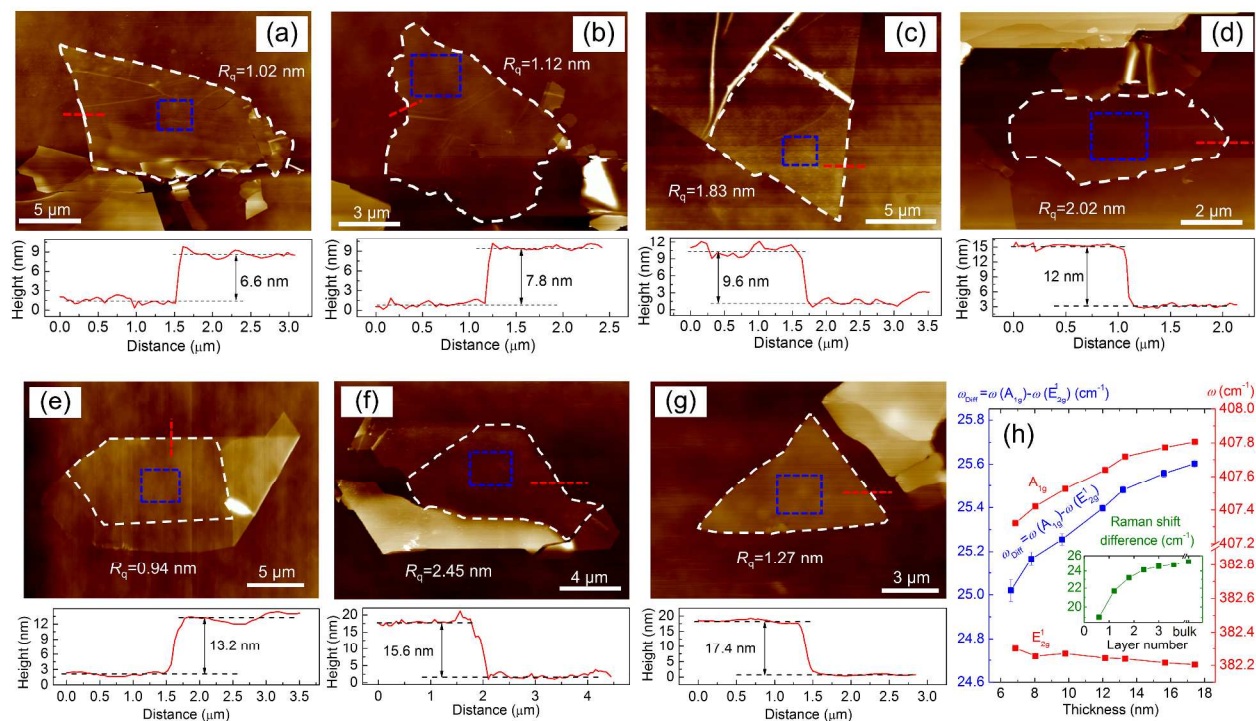


Figure 2. Schematic of the experimental setup for the micro-Raman experiment of MoS₂/c-Si sample. (a) A typical MoS₂/c-Si sample is illuminated by CW and ps 532 nm (2.33 eV) green laser. The laser source could be switched by using a flip mounted mirror. The Raman signals of MoS₂ and c-Si are excited by the same laser and collected by a confocal Raman spectrometer. The laser power is adjusted by a motorized ND filter. The spectrometer and ND filter are controlled by a LabVIEW-based software. (b) The MoS₂ nanosheets are supported on c-Si substrate. Here we use the single-layered MoS₂ to demonstrate the structure. (c) The atomic

structure of MoS₂ from a side view. The big blue balls stand for the Mo atoms, and small yellow balls are Sulphur atoms. The distance between two adjacent layers is around 0.65 nm. (d) Raman spectra of MoS₂ and c-Si are excited by the 532 nm laser in air ambient environment. Temperatures of both MoS₂ and c-Si can be determined simultaneously by their Raman spectra. E_{2g}¹ (~383 cm⁻¹), A_{1g} (~408 cm⁻¹) modes, and c-Si (~519 cm⁻¹) LO phonon mode are observed in our seven samples. Here we choose the E_{2g}¹ mode to evaluate the MoS₂ temperature.

Sample preparation and characterization

We prepare seven few-layered MoS₂ samples by micromechanical cleavage technique (see Material and Methods section for more details). The lateral size of layered MoS₂ nanosheets has an equivalent radius ranging from 2.5 to 6.2 μm. This limited sample size is also considered in our numerical modeling for data processing.



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3 **Figure 3.** (a)-(g) AFM measurement results of seven MoS₂ samples supported on c-Si. The
4 upper images in (a)-(g) show the AFM images. The white dashed circled area indicates the
5 measured MoS₂ sample. The blue dashed box indicates the sample where the Raman experiment
6 is performed. The height profiles shown below the images correspond to the red dashed lines in
7 the above AFM images. The R_q value in each AFM image indicates the RMS roughness. (h)
8 Thickness dependence of Raman shift of two Raman modes in MoS₂ nanosheets (right vertical
9 axis) and their difference (left vertical axis). The two modes shift away from each other with
10 increased thickness. The inset shows the results and prediction based on Lee *et al.*'s work.³⁶

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23 Figure 3 (a)-(g) show AFM images of seven MoS₂ samples supported on c-Si substrate. In each
24 image, we mark the sample area by the dashed white circle. The height profiles shown below the
25 images correspond to the red dashed lines in the AFM images. The samples have a thickness of
26 around 6.6 nm, 7.8 nm, 9.6 nm, 12.0 nm, 13.2 nm, 15.6 nm and 17.4 nm, respectively. The blue
27 dashed square in each sample AFM image shows the area where the laser is focused during
28 different Raman experiments. We also evaluate the sample surface roughness. For example, the
29 6.6 nm thick sample has a root-mean-square (RMS) roughness (R_q) of 1.02 nm. R_q increases a
30 little bit with increased thickness except for 13.2 nm and 17.4 nm thick sample. These two
31 samples may have fewer wrinkles or ripples. Also, the substrate (c-Si) has a R_q of 0.09 nm which
32 confirms its atomically smooth surface. Figure 3(h) displays the thickness dependence of Raman
33 shift of two Raman modes of MoS₂ nanosheets. The Raman shift of E_{2g}^1 mode has a red shift
34 while that of the A_{1g} mode has a blue shift with increased layer number as we found and
35 explained in previous work.¹¹ The Raman shift difference [$\omega_{\text{Diff}} = \omega(A_{1g}) - \omega(E_{2g}^1)$] between
36 these two modes is widely used to determine the layer number of MoS₂ nanosheets.³⁶ So we also

plot ω_{Diff} as a function of the sample thickness as blue curve shows, and ω_{Diff} increases with the thickness of MoS₂. Our results agree well with results and predictions of Lee *et al.*'s work.³⁶

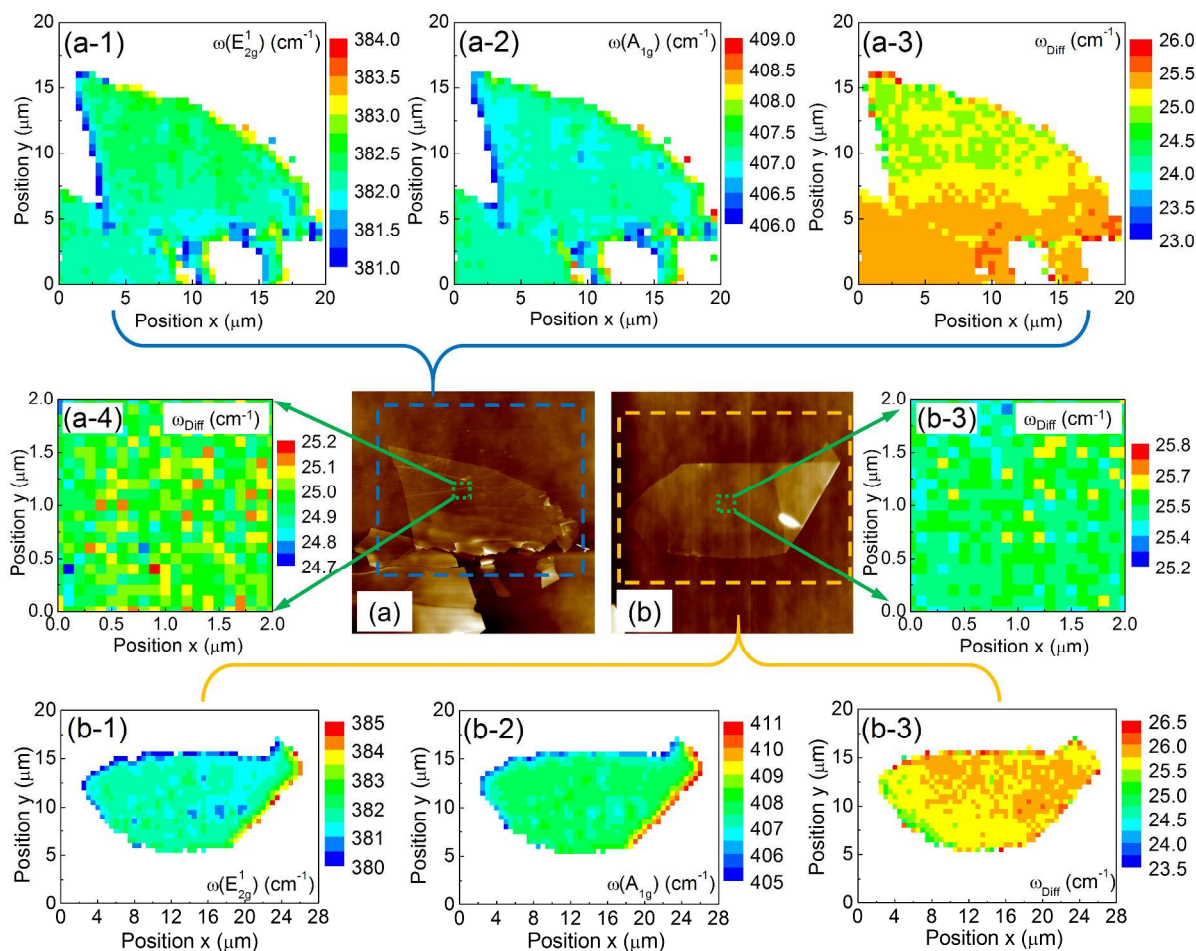


Figure 4. False color images of Raman shift map of 6.6 nm and 13.2 nm thick MoS₂ samples.

The blue and yellow dashed squares in the AFM images (a) and (b) mark the area in which the Raman scan was performed as shown in their sub (1)-(3) figures. (a-1) and (b-1) show the Raman shift mapping from E_{2g}¹ mode, (a-2) and (b-2) show the Raman shift mapping from A_{1g} mode. The Raman shift difference between these two modes are shown in (a-3) and (b-3). The green dashed squares mark the smaller area for detailed mapping as shown in the (a-4) and (b-4).

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3 The small variance of ω_{Diff} shows that the sample thickness is uniform.
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6 We also perform scanning Raman of 6.6 nm and 13.2 nm thick MoS₂ samples to have a better
7 idea of the uniformity of surface structure. Here we take the 6.6 nm thick MoS₂ sample for
8 example to discuss the scanning results. Figure 4(a) shows its AFM image. The blue dashed
9 square marks the area in which the scanning Raman is performed. The square has a width of 20
10 μm . Full Raman spectra are recorded for each point with a step size of 500 nm. The spectra are
11 analyzed by an MATLAB-based automatic fitting program, which determines the Raman shift,
12 intensity, and linewidth for two vibration modes of MoS₂ and LO phonon mode of c-Si. We
13 further process the extracted data to create false color images as depicted in Fig. 4(a-1) and (a-2).
14 Here we set Raman shift information of the bare c-Si substrate as white to increase the contrast
15 between sample and substrate. In these figures, we plot the Raman shift of E_{2g}¹ and A_{1g} modes
16 as a function of position. Figure 4(a-3) shows the Raman shift difference of these two modes.
17 Figure 4(a-4) shows the Raman shift difference from a smaller area as marked with green dashed
18 square in Fig. 4(a). This area is also included in the area where we performed the Raman
19 experiments for *D* and *R* determination. The scanning step size for this area is 100 nm. The
20 relatively uniform Raman shift difference mapping shows the sample thickness is uniform and
21 there is no large interface spacing variance.
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45 **Thermal response of MoS₂ under picosecond and CW laser heating**

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49 In the Raman experiments, for all the seven samples, eight room-temperature Raman spectra are
50 automatically collected at different laser power by the controlled computer to find the laser
51 power coefficient. The CW laser energy is from 1.59 mW to 6.34 mW (0.586 to 2.33 MW/cm²)
52 under the 100 \times objective and from 6.03 to 29.2 mW (0.145 to 0.703 MW/cm²) under the 20 \times
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3 objective. The ps laser energy is from 1.84 to 6.93 mW (pulse power density is from 0.08 to 0.31
4 GW/cm²) under the 50× objective. Note that this laser power is the level just before the laser
5 enters the MoS₂ sample surface. Moreover, the power is maintained as low as possible especially
6 for the ps laser to avoid photon absorption saturation³⁷⁻³⁸ and stay within the linear temperature
7 dependence range for Raman properties. For the 532 nm picoseconds pulse laser heating, the
8 saturation intensity is around 1.13 GW/cm².³⁸ When the photon density exceeds that level, the
9 conductance band will be filled and the material will be unable to absorb further photons
10 according to the Pauli-exclusion principles.³⁹

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12 Here we also take the 6.6 nm thick sample for example to illustrate the results. Five
13 representative room temperature Raman spectra and their corresponding Lorentzian fits of MoS₂
14 and Gaussian fits of c-Si under 100× objective by CW laser are shown in Fig. 5 (a) and under
15 50× objective by ps laser are shown in Fig. 5(b). Also in Fig. 5(a), the inset shows the false color
16 map for the spatial energy distribution of the laser energy beam under 100× objective. The
17 mapping data is from the image captured by a CCD (charge-coupled-device) camera (Olympus
18 DP-26, Olympus Optical Co., Ltd). The corresponding laser spot size (at e^{-1}) on the sample is
19 determined as 0.294 μm. In Fig. 5 (a), both two modes of MoS₂ and LO phonon mode c-Si shift
20 to left (red shift) linearly with increased laser power, and the peak position shifts are visible as
21 $\Delta\omega|(1.59 \text{ mW} \sim 6.34 \text{ mW})$ by CW laser and $\Delta\omega|(1.84 \text{ mW} \sim 4.68 \text{ mW})$ by ps laser for MoS₂.
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23 The temperature rise of c-Si is not very visible due to its larger thermal conductivity, so the
24 Raman shift changes little. The Raman shift changes indicate that the local temperature of the
25 sample becomes higher under a higher laser power.
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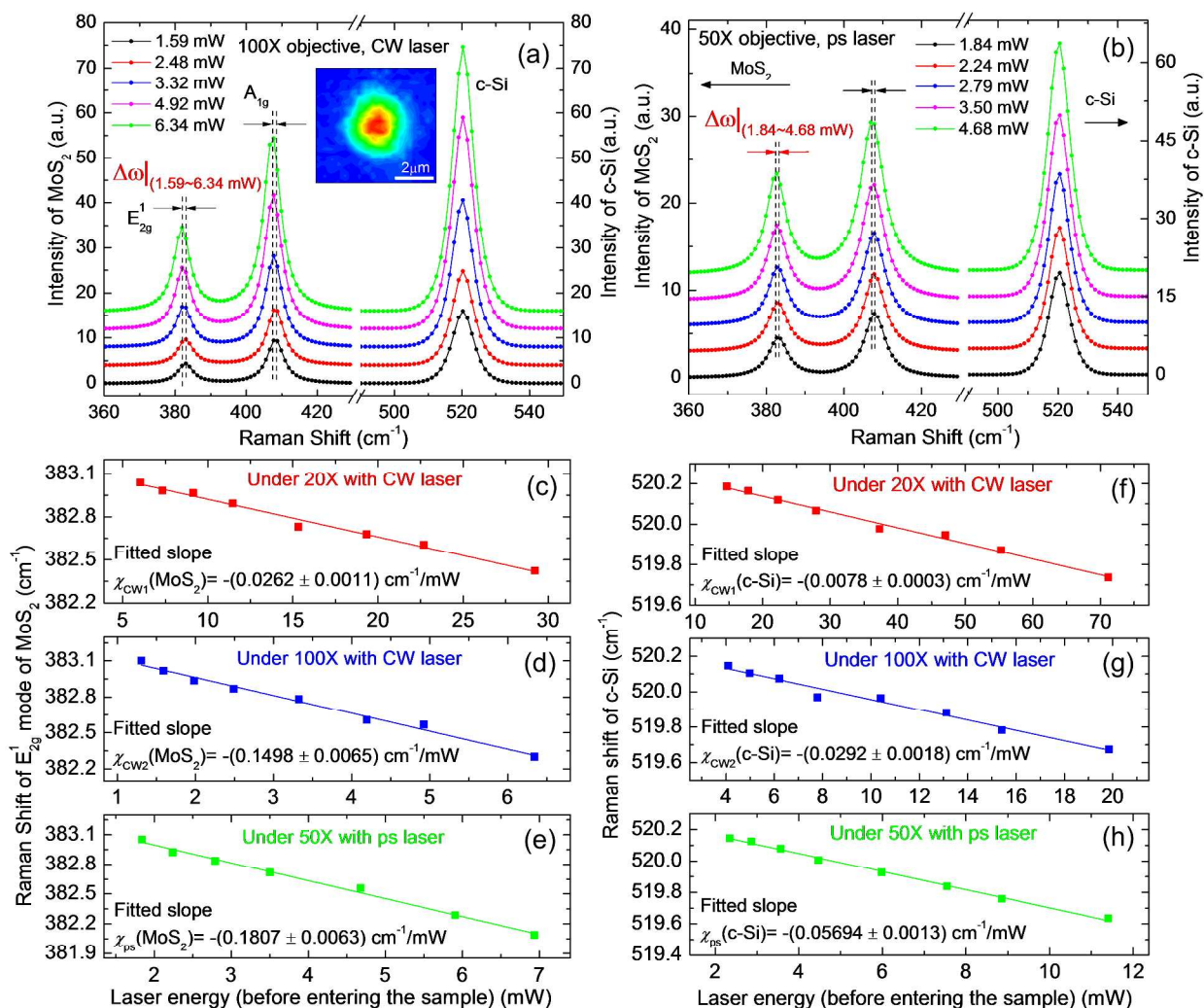


Figure 5. The Raman spectra of MoS₂ nanosheets and the c-Si substrate. The sample with a thickness of 6.6 nm is used as an example to illustrate the ET-Raman experiment results. We use two different objective lenses to generate different laser heating phenomena and different laser sources to generate different energy transport states. The local temperature increases when the laser power increases for both CW laser and ps laser. (a) Five representative Raman spectra of MoS₂ and c-Si at increased excitation laser power under 100× objective with CW laser in the ambient environment. The inset shows the false color map for the spatial energy distribution of the laser energy beam under 100× objective. Here we shift the spectra to increase the clarity for

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3 both (a) and (b). The Raman shifts for two modes of MoS₂ with CW laser are visible as
4 $\Delta\omega$ (1.59 mW ~ 6.34 mW) in (a). The temperature rise for c-Si is not very visible because
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6 Raman shift changes little due to its large thermal conductivity. With CW laser, the Raman shift
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8 for E_{2g}¹ mode of MoS₂ and c-Si as a function of laser power under 20× are shown in (c) and (f),
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10 and under 100× objective is shown in (d) and (g), respectively. The fitting results (solid lines) for
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12 linear power coefficient χ_p are shown in these figures. (b) Five representative Raman spectra of
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14 MoS₂ and c-Si at increased excitation laser power under 50× objective with ps laser heating in
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16 the ambient environment. The Raman shifts for two modes of MoS₂ vs ps laser power are visible
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18 as $\Delta\omega$ (1.84 mW ~ 4.68 mW) in (b). The Raman shift for E_{2g}¹ mode of MoS₂ and c-Si as a
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20 function of laser power under 50× objective with the ps laser power are shown in (e) and (h),
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22 respectively.
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32 Two objective lenses with CW laser are used to generate different optical heating phenomena. In
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34 our specified laser power range for both CW and ps laser, it is observed that the Raman shift
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36 linearly depends on the laser power by $\Delta\omega = \omega(P_2) - \omega(P_1) = \chi(P_2 - P_1) = \chi\Delta P$. χ (cm⁻¹/mW)
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38 is the first-order Raman shift power coefficient (RSC) for two vibration modes of MoS₂ and c-Si,
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40 and P (mW) is the laser power. In this work, we choose the Raman results from this E_{2g}¹
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42 vibration mode to deduce RSC because the in-plane E_{2g}¹ mode will be less affected by the
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44 interlayer interactions and weakly affected by the substrate.⁴⁰ Besides, the E_{2g}¹ mode exhibits
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46 slightly polar dependence on the laser polarization configuration. So the effects of switching
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48 laser sources on Raman results will be eliminated. By CW laser, as shown in Fig. 5(c) and (d),
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50 the linear fitting results RSC of MoS₂ E_{2g}¹ mode under 20× objective is $-(0.026 \pm 0.001)$ cm⁻¹
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3 $^1/\text{mW}$, and under $100\times$ objective is $-(0.150\pm 0.007) \text{ cm}^{-1}/\text{mW}$. The RSC value of c-Si, as shown
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5 in Fig. 5(f) and (g), under $20\times$ objective is $-(0.008\pm 0.001) \text{ cm}^{-1}/\text{mW}$, and under $100\times$ objective
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7 is $-(0.029\pm 0.002) \text{ cm}^{-1}/\text{mW}$. The power coefficient under $100\times$ objective ($\chi_{\text{CW}2}$) is larger than
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9 that under $20\times$ objective ($\chi_{\text{CW}1}$). We attribute this to the fact that the temperature rise increases
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11 more rapidly under $100\times$ objective due to its higher power density (small laser spot size).
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13 Besides, the linear dependence on the laser power for two different heating sizes indicates that
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15 there are no significant changes in the thermal properties of materials in our considered laser
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17 power range. By ps laser under $50\times$ objective, as shown in Fig. 5(e) and (f), the RSC values of
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19 MoS_2 E_{2g}^1 mode and c-Si are $-(0.181\pm 0.006) \text{ cm}^{-1}/\text{mW}$ and $-(0.057\pm 0.001) \text{ cm}^{-1}/\text{mW}$,
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21 respectively. Also, RSC values for other six samples are summarized in Table S1. The RSC
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23 values roughly increase with increased MoS_2 thickness for both CW and ps laser heating. The
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25 main reason is that the thicker sample will absorb more energy when the thickness is smaller
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27 than its laser absorption depth, so a higher temperature rise will be expected. Under same laser
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29 power level (1 mW before it enters the sample), the Raman wavenumber change will increase.
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39 **Determination of D and R**

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42 Then a 3D numerical modeling based on the finite volume method is conducted to calculate the
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44 temperature rise to determine the hot carrier diffusion coefficient (D) and the interface thermal
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46 resistance (R). The modeling setup is shown in Figure. 6(a). (see Materials and Methods section
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48 for more details) Specially, τ is set as 1 ns at room temperature.³⁰ For MoS_2 , the photo-excited
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50 electrons have a life time of hundreds of picoseconds in few-layered samples and nanoseconds or
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52 longer in the thick crystal.²⁹⁻³⁰ This effect will be discussed latter in this work. Besides, for
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54 phonon contribution to the thermal transport, the material thermal conductivity could be reduced
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if the heating size is comparable to, or smaller than the phonon mean free path.⁴¹⁻⁴² In this work, for MoS₂, the phonon mean free path is less than 20 nm⁴³⁻⁴⁴ which is much smaller than the laser spot size (radius: 0.294 to 1.15 μm). So the ballistic effect on thermal conductivity is not influential. In this 3D modeling, we only consider the diffusive phonon transport.

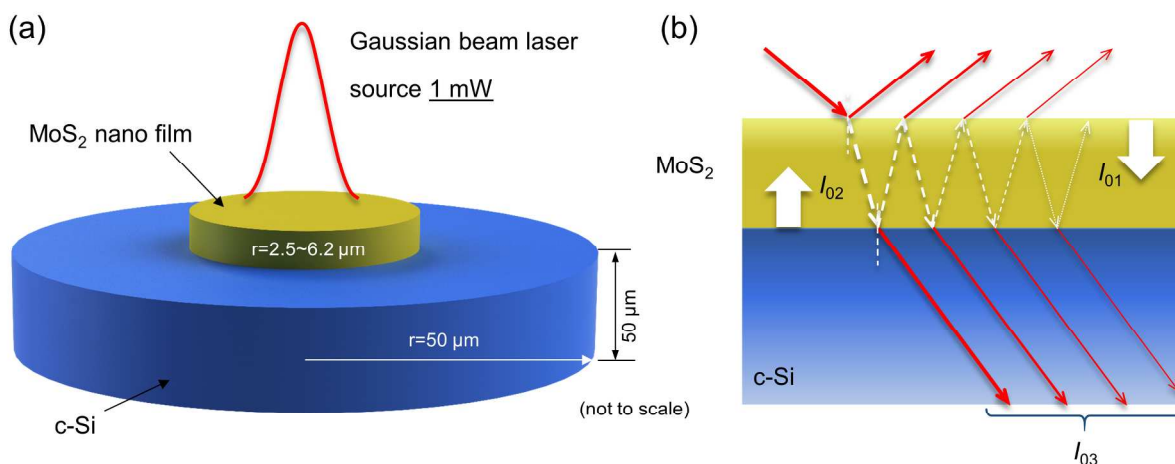


Figure 6. (a) 3D numerical modeling setup. The computational domain of the substrate has a radius and thickness of $50 \mu\text{m}$; the MoS₂ sample has the real size. Both CW and ps laser have a Gaussian beam and the same spot size as the experiment. Laser energy is 1 mW before the laser enters the sample surface. (b) When laser beam irradiates the sample surface, multiple reflections happen at the interface between MoS₂ and c-Si. The transmitted power at the top surface (I_{01}), the reflected power at the bottom surface (I_{02}) of MoS₂ and the transmitted power in the c-Si top surface (I_{03}) are calculated out according using the Transfer Matrix Method (TMM).⁴⁵

When a laser beam irradiates the sample surface, multiple reflections happen at the interface between MoS₂ and c-Si as shown in Figure 6(b). Based on the optical properties of these two materials and the Transfer Matrix Method (TMM),⁴⁵ we could determine the transmitted power at the top surface (I_{01}), the reflected power at the bottom surface (I_{02}) of MoS₂ and the

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3 transmitted power in c-Si top surface (I_{03}). As mentioned in the introduction section, our method
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5 could eliminate the errors from the local laser absorption evaluation and temperature coefficient
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7 calibration. The normalized RSC value has no effect of the Raman temperature coefficient, but
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9 has conjugated laser absorption effect from MoS₂ and Si. Further data reconstruction is needed to
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11 completely rule out the dependence on laser absorption. This is given in Supporting Information
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13 S2 with detailed explanations. Take the 6.6 nm thick MoS₂ for example, from the 3D numerical
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15 simulation and Raman experiment, we could calculate Θ_1 and Θ_2 for MoS₂ in the (D , R) space.
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17 Especially, in the (D , R) space for the zero-transport state, temperature rises for MoS₂ and Si
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19 remain constant without changing other parameters. Note in our Raman experiment, as
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21 mentioned above, the measured RSC of both MoS₂ and c-Si are Raman-intensity weighted
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23 average of the sample. At a location of the sample, the local Raman intensity is proportional to
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25 the local laser intensity and the scattered Raman signal multi-reflected in the sample. For the
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27 zero-transport state, the measured temperature rise is also time averaged over the pulse width.
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29 All these have been considered in our modeling to evaluate the temperature rise of both MoS₂
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31 and c-Si substrate.
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40 Figure 7 (a) and (b) show the calculated normalized RSC mapping for MoS₂. The experimentally
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42 obtained normalized RSC (the isolines) could be satisfied by many different (D , R) pairs. In both
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44 cases, the lower D or higher R implies a higher normalized RSC value (temperature rise). When
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46 D decreases, the heating area will be more confined to the laser heating region that results in a
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48 higher local temperature rise and difference. When R increases, under the same temperature drop,
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50 less heat could dissipate from MoS₂ to c-Si substrate. Additionally, in Fig. 7 (a) (under 20×
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52 objective), the normalized RSC value is less sensitive to the D change. However, this sensitivity
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54 increases under 100× objective in Fig. 7 (b). As we discussed in the physical model, when the
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3 laser spot size is comparable to, or smaller than the carrier diffusion length, the hot carriers could
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5 diffuse out of the heating area more easily and their effect becomes more prominent.
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9 We could determine the exact D and R values by combining the results from these two cases as
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11 shown in Fig. 7 (c), the cross point of the blue (Θ_1) and dark red (Θ_2) dashed curves: D is 0.637
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13 cm^2/s and R is $1.75 \times 10^{-7} \text{ K} \cdot \text{m}^2/\text{W}$. As discussed in our previous work,⁵ we use the normalized
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15 probability distribution function (Ω) to present the final results uncertainty as shown in the false
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17 color map of Fig. 7 (c). $\Omega = \exp\left[-(x - \bar{x})^2 / (2\sigma^2)\right]$ with x as the variable, \bar{x} as its average, and
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19 σ is the standard deviation. In the (D, R) space, we have $\Omega_{(D,R)} = \Omega_{\Theta_1} \cdot \Omega_{\Theta_2}$. The value of
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21 $\Omega_{(D,R)} = 0.6065$ corresponding to the σ confidence in the (D, R) space is used to show the final
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23 results uncertainty. Finally, the deduced R is $1.75^{+0.08}_{-0.08} \times 10^{-7} \text{ K} \cdot \text{m}^2/\text{W}$ and D is $0.637^{+0.193}_{-0.154} \text{ cm}^2/\text{s}$.
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25 Also, the final results and the uncertainty for the other six samples are summarized in Table 1
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27 and also plotted in Figure 8 (a) and (b). Our above uncertainty analysis only considers the
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29 uncertainty in our characterization. In this work, the in-plane thermal conductivity data of MoS_2
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31 is taken from literatures. We also have conducted analysis to study how sensitive D and R are to
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33 the uncertainty carried by k_{\square} (see section S6 in Supporting Information). We find that R is not
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35 sensitive to the uncertainty in k_{\square} , but D is very sensitive. D decreases by 16.6% if k_{\square} is increased
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37 by 10%. This is understandable since k_{\square} and D both contribute to in-plane thermal transport. It is
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39 conclusive that the heat transfer induced by hot carrier diffusion is less than that by in-plane heat
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41 conduction.
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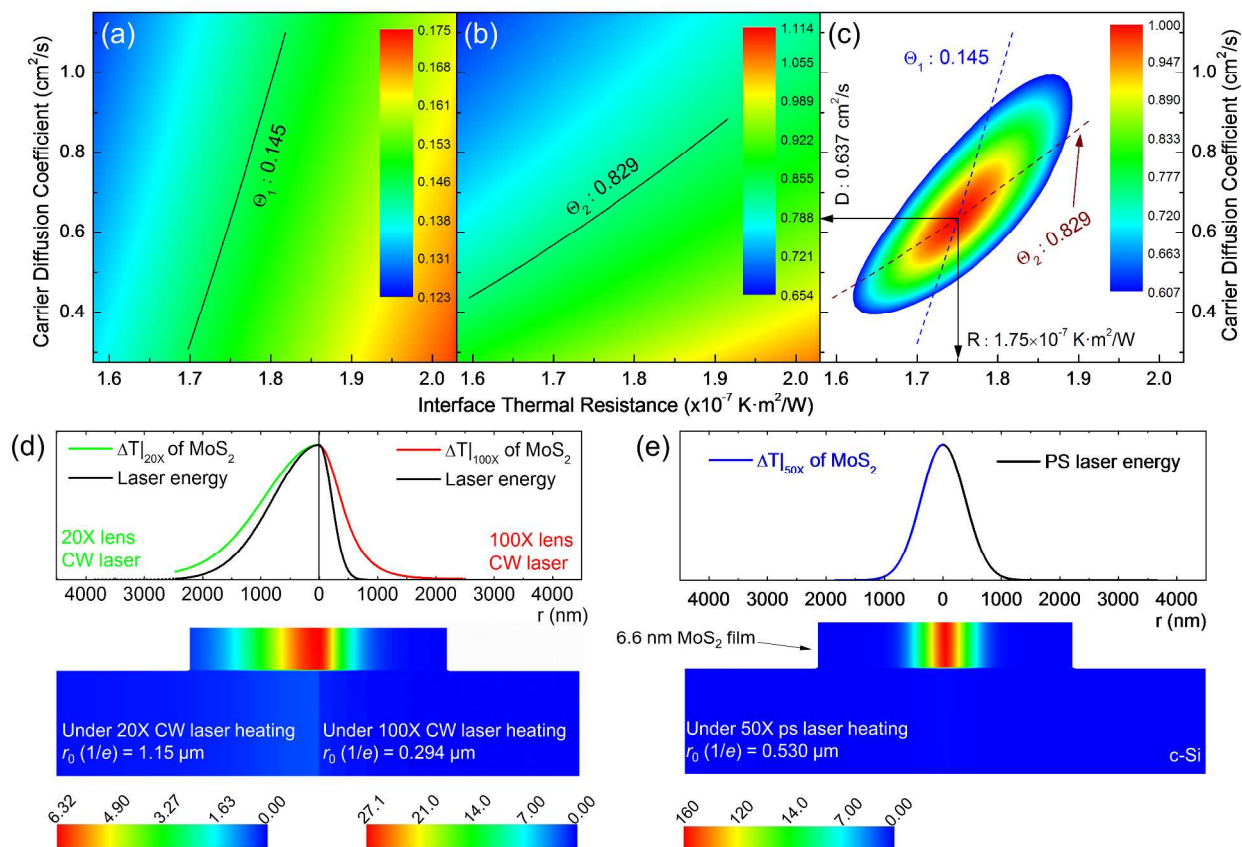


Figure 7. 3D numerical modeling results for the 6.6 nm thick MoS₂ sample to illustrate the temperature distribution. The normalized RSC (Raman shift power coefficient) Θ for different values of D and R is shown in (a) under the 20 \times objective and in (b) under 100 \times objective. The experimentally obtained $\Theta_1=0.145$ and $\Theta_2=0.829$ are shown in these two figures. (c) Determined D and R as well as the uncertainty region. The normalized probability distribution function (Ω) contour shows the uncertainty distribution: 0.6065 is for the σ confidence. Based on the determined D and R for this sample, the calculated temperature rise distribution and laser energy distribution in the 6.6 nm MoS₂ sample on c-Si substrate under CW laser heating with 20 \times and 100 \times objectives are shown in (d), and under ps laser heating with 50 \times objective in (e).

Table 1. The summary of the hot carrier diffusion coefficient (D) from the 3D numerical modeling and data fitting, and the corresponding electron mobility (μ) and hot carrier diffusion length (L_D). Also, the calculated the interface thermal resistance (R).

Sample Thickness	D (cm ² /s)	μ (cm ² /V·s)	L_D (μ m)	R (10^{-7} K·m ² /W)
6.6 nm	$0.637^{+0.193}_{-0.154}$	$25.5^{+7.71}_{-6.18}$	$0.252^{+0.139}_{-0.124}$	$1.75^{+0.08}_{-0.08}$
7.8 nm	$0.768^{+0.227}_{-0.210}$	$30.7^{+11.1}_{-8.41}$	$0.277^{+0.166}_{-0.145}$	$1.87^{+0.10}_{-0.09}$
9.6 nm	$0.753^{+0.201}_{-0.166}$	$30.1^{+8.04}_{-6.62}$	$0.274^{+0.142}_{-0.129}$	$1.51^{+0.06}_{-0.06}$
12.0 nm	$0.945^{+0.262}_{-0.209}$	$37.8^{+10.5}_{-8.37}$	$0.307^{+0.162}_{-0.145}$	$1.64^{+0.08}_{-0.07}$
13.2 nm	$1.07^{+0.31}_{-0.25}$	$42.7^{+12.6}_{-10.0}$	$0.327^{+0.177}_{-0.158}$	$1.29^{+0.06}_{-0.06}$
15.6 nm	$0.825^{+0.208}_{-0.176}$	$33.0^{+8.34}_{-7.02}$	$0.287^{+0.144}_{-0.132}$	$1.30^{+0.05}_{-0.04}$
17.4 nm	$1.25^{+0.31}_{-0.26}$	$50.0^{+12.5}_{-10.3}$	$0.354^{+0.177}_{-0.161}$	$1.22^{+0.06}_{-0.06}$

To visualize hot carrier diffusion effect on the thermal distribution, we calculate the temperature rise distribution for the 6.6 nm thick MoS₂ sample under CW laser heating with 20 \times (left part) and 100 \times (right part) objectives by the determined D and R and show the results in Fig. 7(d). For both cases, the temperature rise is quite uniform in the thickness direction, and the heat conduction along the thickness direction is much larger than that in the in-plane direction in MoS₂ due to its large ratio of lateral size/thickness. Because of the high thermal conductivity of c-Si, the temperature rise of c-Si is very small. Compared with the laser energy distribution (dark curve), the temperature distribution of MoS₂ is out of the laser spot a lot, especially for the small heating size (100 \times objective). As discussed above, the diffusion length L_D (252 nm for 6.6 nm thick MoS₂) is only 1/5 of r_0 under 20 \times objective (1.15 μ m) and almost same to that under 100 \times

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3 objective (294 nm). This makes the hot carrier diffusion effect on heat transport more prominent
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5 under 100× objective. For the zero-transport state ps laser heating, as shown in Fig. 7(e), the
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7 temperature rise of MoS₂ has almost the identical distribution to the ps laser energy distribution.
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9 The temperature rise of c-Si is so small due to its large volume and long laser absorption depth
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11 (~820 nm). This confirms that the *R* and *D* have negligible effect on the temperature rise of the
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13 samples.
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18 As discussed above in the physical model section, during the diffusion process, electrons (*e*) and
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20 holes (*h*) move as pairs due to the Coulomb attraction between them. So the measured *D* is the
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22 ambipolar diffusion coefficient, $D = 2D_e D_h / (D_e + D_h)$, where $D_{e(h)}$ is the unipolar diffusion
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24 coefficient of electrons (holes).⁴⁶ However, equal numbers of electrons and holes are generated,
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26 and the effective masses of electrons and holes of MoS₂ are comparable and even similar in our
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28 optical study.⁴⁷ Therefore, both D_e and D_h are assumed to be same. As a result, we can
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30 approximately treat the determined *D* in this work as unipolar carrier diffusion coefficients of
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32 both electrons and holes. Besides, the diffusion coefficient is related to the mobility (μ) by the
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34 Einstein relation in this thermalized system as $D/k_B T = \mu/q$, where k_B , *T*, and *q* are the
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36 Boltzmann constant, temperature, and the charge of each carrier. Here, we assume that the
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38 carriers have a thermal distribution of 300 K during the diffusion process because the energy
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40 relaxation time is only several picoseconds.³⁰ For the 6.6 nm thick MoS₂ nanosheets sample, the
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42 measured *D* corresponds to a mobility of $\mu=25.5$ cm²/Vs. Moreover, 17.4 nm thick MoS₂ has
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44 $\mu=50.0$ cm²/Vs. Our measured μ is very close to the literatures value of 30-60 cm²/Vs for few-
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46 layered MoS₂ on SiO₂,¹⁵ ~70 cm²/Vs for few-layered MoS₂ on Al₂O₃.⁴⁸ One of the biggest
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48 difference between the optical and electric methods to study the carrier movement is that we do
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3 not cover the sample (MoS₂ nanosheets) with a dielectric layer such as HfO₂.³⁴ Nevertheless, our
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5 optically measured mobility is still comparable to that measured using the contact methods. As
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7 described above, during the diffusion process, the electron-hole pair moves together so that the
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9 pair is electrically neutral and will not be influenced by the Coulomb scattering.²⁰ Hence, our
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11 results are much smaller than the theoretical optical-phonon-scattering-limited mobility (~400
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13 cm²/Vs).⁴⁹ Such high mobility could only be approached by adopting high- κ dielectric materials
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15 (*e.g.*, HfO₂, Al₂O₃) to build top-gated devices.^{34, 50} The dielectric layer is believed to affect
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17 (boost) the mobility because of the suppression of Coulomb scattering by the dielectric.⁵¹⁻⁵²
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19 Besides, it has been shown that some of the reported mobility values may have been greatly
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21 overestimated in this top-gated geometry.⁵³
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28 **Effect of MoS₂ thickness on R and D**

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31 In order to elucidate how R and D values change with MoS₂ thickness, we plot them as a
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33 function of MoS₂ thickness as shown in Fig. 8 (a)(b). The detailed results are also summarized in
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35 Table 1. Both uncertainties come from the RSC fitting procedure and do not include systematic
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37 errors from the uncertainty of P , r_0 and NA. Especially, D has a relatively higher uncertainty
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39 than R . In this work, the hot carrier transport is characterized by its effect on thermal energy
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41 distribution. To differentiate the R and D effect, we design two steady states with different laser
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43 heating sizes. As a result, the hot carrier effect could be very prominent with an ultra small
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45 heating size and negligible with very large heating size. Ideally, if we could have two extreme
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47 heating size and negligible with very large heating size. Ideally, if we could have two extreme
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49 heating states (very large and very small laser spot size), the uncertainty of D could be strongly
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51 reduced. In Fig. 8 (b), the carrier diffusion coefficient D is higher for thicker MoS₂ samples. D
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53 value almost doubles from 6.6 nm to 17.4 nm MoS₂ sample. A similar trend for this thickness-
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55 dependent D value is also found by Li *et al* ⁵⁴. This strong dependence may be attributed to
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weaker in-plane electron-phonon interaction for thicker samples.⁵⁵ Besides, the additional MoS₂ layers could serve as a dielectric capping layer which enhances screening of long-range disorder.^{15, 54-55} And as the thickness increases, it has also been found that the effect of the charge impurities can be mitigated to some extent which leads to a mobility enhancement.⁵⁶

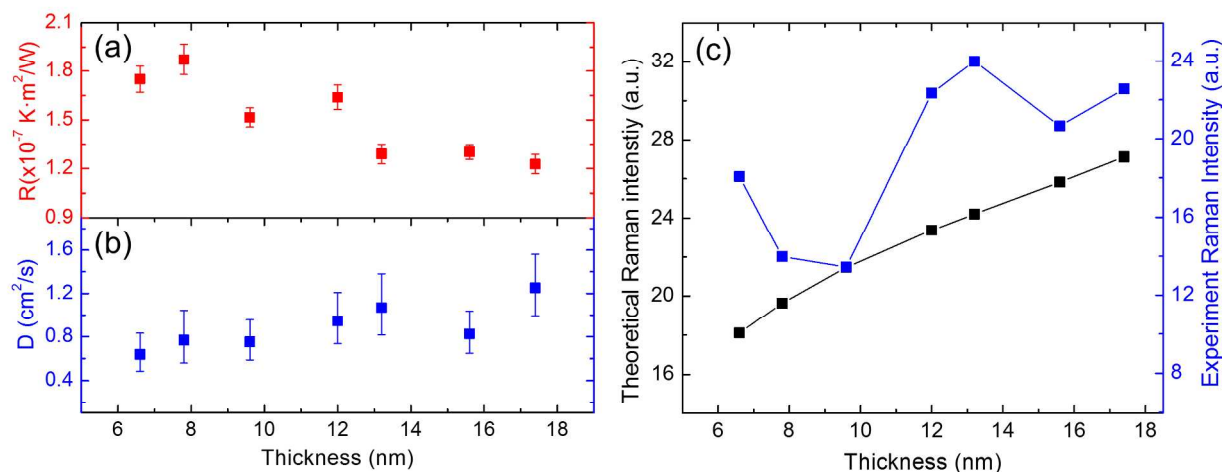


Figure 8. (a) Interface thermal resistance: R , (b) hot carrier diffusion coefficient: D of seven MoS₂ samples supported on c-Si. (c) The comparison of the experiment Raman peak intensity trend of MoS₂ E_{2g}^1 mode and the theoretical Raman intensity F for the seven samples.

The interface thermal resistance we obtain here is in the order of $1.5 \times 10^{-7} \text{ K}\cdot\text{m}^2/\text{W}$. They are larger than what we found in previous work, such as the 8.4 nm MoS₂ on c-Si with R is $7.66 \times 10^{-8} \text{ K}\cdot\text{m}^2/\text{W}$.¹¹ We attribute this mainly to the unknown errors in laser absorption evaluation and Raman temperature coefficient calibration in our previous work while the ET-Raman completely eliminates the errors from laser absorption evaluation and temperature coefficient calibration. We feel the laser absorption is one of the factors giving the largest uncertainty. First of all, in our previous work and work reported in literatures by other researchers, the laser beam absorption

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3 was evaluated based on the refractive index of MoS₂ as 4.4. However, this property features very
4 large deviations from sample to sample, and a broad range of 3.05~5.20 has been reported in
5 literatures.²⁷⁻²⁸ Second, a small spacing between the 2D material and the substrate can induce
6 strong optical interference and change the absorption behavior substantially (detailed in the next
7 section). Unfortunately, quantitative knowledge of this spacing is still not available, and this
8 significantly downgrades the measurement accuracy. Third, when calculating laser beam
9 absorption, the laser is assumed normal to the 2D material in past work. In fact, the laser beam is
10 focused with a finite numerical aperture. This could bring in great errors in laser absorption
11 calculation. The smaller R of thicker samples reveals their better interface contact with the
12 substrate, leading to accordingly improved interfacial energy coupling as found in our previous
13 work.¹¹

30 **The effect of optical properties**

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33 To further elaborate that the optical properties [the complex refractive index ($n-ik_L$)] of the
34 sample have no effect on the results from ET-Raman technique, we vary the n and k_L values to
35 calculate the laser absorption rate based on TMM as shown in Table S2. In the above 3D
36 numerical simulation, the preset complex refractive index for 6.6 nm MoS₂ is 4.4-1.1*i*.²⁷ Based
37 on different combinations of n and k_L values of MoS₂, we calculate the temperature rise ΔT_1 to
38 ΔT_6 and deduce $\Theta(\text{MoS}_2)$ [from Eq. (S9) in Supporting Information S2] for both 20 \times and 100 \times
39 objectives (two sub-states). $\Theta(\text{MoS}_2)$ has a variance of less than one thousandth while changing
40 n or k_L value as shown in Table S2. For example, we reduce n by half and keep k_L value (2.2-
41 1.1*i*), the calculated $\Theta(\text{MoS}_2)$ only increases by 0.11%. So the change could be neglected.
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57 Because the R and D values are determined from $\Theta(\text{MoS}_2)$ under 20 \times and 100 \times objectives, so it
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3 is conclusive that the ET-Raman technique could eliminate the errors brought in by optical
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5 absorption evaluation.
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9 As discussed above, the optical properties of the samples are difficult to accurately determine
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11 and vary a lot from sample to sample. Additionally, based on the determined optical properties,
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13 the laser absorption rate is estimated assuming a vertical incident laser beam. However, the
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15 focused laser beam converges along the propagation direction and this is very complicated to be
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17 taken into account when evaluating the laser absorption level. For monolayer MoS₂, the
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19 absorbance level experimentally determined varies from 4% to 9%.⁵⁷⁻⁵⁸ Among the error sources
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21 for Raman-based thermal probing technique, the relative error in the laser absorption was by far
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23 the dominant contributor. Moreover, the accuracy of the measurement is strongly limited by the
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25 uncertainty of the optical absorption evaluation. To this end, some measured the laser absorption
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27 level by themselves to consider the absorption variation among samples⁵⁹ or discussed the results
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29 by referring different absorbance levels obtained from others.³⁵ All of these treatments still have
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31 to consider the effects and errors from optical absorption evaluation so that our results provide
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33 the most accurate understanding to date.
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40 **The effect of the thickness on interface energy transport: interpretation from interface** 41 **structure** 42 43 44

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46 As we briefed above, the MoS₂-substate interface could have a small spacing, and this spacing
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48 will significantly change the laser absorption in MoS₂. This effect has not been considered in the
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50 past for laser absorption evaluation. Our ET-Raman technique completely rules out this effect.
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52 To have a deeper understanding of this effect, and shed light on above interfacial thermal
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54 resistance results, we perform the Raman intensity enhancement study to reveal the interface
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3 structure. As has been investigated, the local interfacial energy coupling will decrease
4 significantly if there is even a tiny spacing (*e.g.* 0.1 nm) at the interface.^{11, 24} At the same time,
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6 the spacing will induce Raman intensity variation. So in this section we study the Raman
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8 intensity of the MoS₂ sample against its thickness, in anticipation to uncover the local interface
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10 spacing information.
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16 Figure 8(c) shows the comparison of the experiment Raman peak intensity of MoS₂ E_{2g}¹ mode
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18 and the theoretical Raman intensity F for our seven MoS₂ samples (see the calculation details for
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20 F in the Supporting Information S7). In the comparison, we assume that there is no spacing for
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22 9.6 nm thick MoS₂ sample since it has the lowest theoretical Raman intensity among the seven
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24 samples. The deviation of the calculation results from our experiment results confirms the
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26 spacing existence for other six MoS₂ samples, especially for the 6.6 nm and 13.2 nm thick ones.
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28 This spacing can significantly increase the interface thermal resistance and local laser energy
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30 absorption. For the first four samples (6.6 ~ 12.0 nm thick), the 9.6 nm thick sample has the
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32 lowest R value due to its perfect interface contact (assumed no spacing). Additionally, the
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34 thermal expansion coefficient (TEC) of MoS₂ nanosheets ($\sim 10^{-5} \text{ K}^{-1}$)⁶⁰⁻⁶¹ is larger than that of c-
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36 Si ($3.9 \times 10^{-6} \text{ K}^{-1}$)⁶². Also during the experiment, MoS₂ will have a higher temperature rise than c-
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38 Si. So when the sample is under laser heating, these two factors (spacing existence and TEC
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40 mismatch) combine to lead to interfacial thermal expansion mismatch between MoS₂ nanosheets
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42 and c-Si. This could result in increased local interface spacing, less efficient heat transfer, and a
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44 higher interfacial thermal resistance. For the last four samples (12.0 ~ 17.4 nm thick), the R value
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46 has a declining trend. We attribute this to the fact that thicker MoS₂ samples may have smaller
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48 TEC value just like PET (polyethylene terephthalate) film.⁶³ The TEC mismatch between MoS₂
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50 nanosheets and c-Si substrate therefore decreases. As a result, the local interface spacing increase
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3 during experiment will become smaller than the thinner samples, leading to a better interface
4 energy coupling. On the other hand, as we studied before,¹¹ thicker samples have better
5 mechanical stiffness which could help form a better contact with c-Si substrate during sample
6 preparation. This could also account for the reduced R for thicker samples in this work.
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13 Additionally, for some Raman-based thermal probing techniques used in literatures,³⁵ the TEC
14 mismatch could also introduce large errors in the Raman temperature coefficient calibration.
15 During the laser heating, the temperature rises of two materials are different. Especially, the
16 temperature rise of c-Si is pretty small due to its large thermal conductivity. As a result, the two
17 materials will experience different mechanical stresses. However, during the calibration
18 experiment, they are kept at the same temperature level. Therefore, the thermal expansion
19 mismatch between the two materials are different in calibration and experiment. As a result, the
20 Raman wavenumber changes caused by the stress in MoS₂ during the calibration are very
21 complicated to be examined. Fortunately, as mentioned above, we do not need the Raman
22 temperature calibration results for ET-Raman technique. So this kind of errors could be
23 completely ruled out.
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40 **The dependence of hot carrier diffusion coefficient D on the carrier lifetime τ**

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44 The carrier lifetime τ takes 1 ns in our data processing by solving Eqs. (1) and (2). So the finally
45 determined D is actually dependent on the τ value. To further expound this effect, as we did
46 before,⁵ a normalized hot carrier concentration $\xi = \Delta N / \tau$ is defined and used to re-express those
47 equations as (by neglecting the thermal activation term):
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$$53 \quad D\tau\nabla^2\xi - \xi + \Phi\alpha = 0, \quad (5)$$

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$$k_T \nabla^2 \Delta T + (h\nu - E_g) \Phi \alpha + E_g \xi = 0. \quad (6)$$

From these two new equations, term $D\tau$ could be determined without knowing other hot carrier properties. In this work, the carrier diffusion coefficient D is determined based on the carrier lifetime τ . However, the interface thermal resistance R has no dependence on that. The lifetime diffusion length of the hot carriers is evaluated from D and τ as $L_D = \sqrt{\tau D}$. As summarized in Table 1, L_D of seven MoS₂ samples is in the order of 300 nm. Such results are in good agreement with others' work. Wang *et al.* have deduced D around 20 cm²/s, τ around 0.1 ns, and the corresponding L_D around 450 nm for 1.5~2.2 nm thick MoS₂ on SiO₂/Si measured by spatially and temporally resolved pump-probe technique.²⁰ Also, Kumar *et al.* have shown that bulk MoS₂ on SiO₂ has L_D around 275 nm with τ around 180 ps measured by a transient absorption microscopy study.³⁴ We thus firmly conclude that the ET-Raman can securely determine the hot carrier lifetime diffusion length. The diffusion coefficient is dependent on the lifetime data, which needs to be obtained from a separate experiment.

Applicability of ET-Raman technique

This ET-Raman technique could also be applicable for other sample structures, such as suspended 2D material. For this structure, the absorbed laser energy could only dissipate along the in-plane direction. Additionally, the sample thermal relaxation time will be longer and there could be a heat accumulation effect by laser pulses. Therefore, the sample could be easily destroyed during the first several laser pulses. However, by controlling the laser to have a longer cooling time between pulses (low repetition rate), we could still apply ET-Raman to characterize suspended 2D materials. By using two different laser heating sizes in steady state laser heating, and one state in pulsed laser (nanosecond or picosecond laser) heating, both in-plane thermal

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3 conductivity and hot carrier diffusion coefficient could be determined.
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6 We can also use ET-Raman to study other 2D materials, such as TMDs, black phosphorus, and
7 graphene. However, the following points should be paid attention to. First, for materials with an
8 indirect bandgap, like few-layered MoS₂, the radiative recombination of carriers is strongly
9 restricted so that the energy carried by the hot carriers will be transferred to local phonons. For
10 these materials, we could just apply ET-Raman demonstrated in this work to determine their D
11 and R values. Second, for materials with a direct bandgap, such as single-layer MoS₂, the
12 radiative transitions dominate the recombination process. A coefficient may be applied to the last
13 term of Eq. (2) to describe how much energy could transfer to local phonons. Third, for the
14 materials without bandgap, like graphene, no hot electrons are generated during laser excitation.
15 Electrons will carry the photon energy and transfer the energy to local lattice by electron-phonon
16 scattering. So heat conduction equations for both electron and phonon will be needed to describe
17 the diffusion process. Last, under extreme cases, e.g. the material has a very long or very short
18 hot carrier diffusion length compared with the laser heating spot size, the hot carrier diffusion
19 coefficient D will become difficult to measure.
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40 **Conclusion**

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44 As exemplified by studying the hot carrier diffusion coefficient (D) and the interface thermal
45 resistance (R) of mechanically exfoliated MoS₂ nanosheets on the c-Si substrate, we demonstrate
46 a novel technique: ET-Raman without evaluation of light absorption or absolute temperature rise
47 of MoS₂. The hot carrier effect on heat conduction could significantly extend the heating area,
48 especially when the laser heating size is comparable to the hot carrier diffusion length. The laser
49 focal spot size was varied from 0.294 μm to 1.14 μm to change hot carrier effect in heat
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3 conduction, and the resulting temperature rise effect was measured by power differential of
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5 Raman shift. Instead of only using continuous laser, a picosecond pulsed laser was also applied
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7 to heat and excite the Raman signal. By studying MoS₂ and the substrate's thermal response
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9 under different laser heating states, *D* and *R* were determined without knowing the laser
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11 absorption or the temperature coefficients of MoS₂. This development successfully eliminates the
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13 weak points of currently widely used Raman-based thermal characterization techniques. For our
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15 seven MoS₂ samples, under the 1 ns hot carrier lifetime, their hot carrier diffusion coefficient
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17 was measured in the order of 1.0 cm²/s which corresponds to a diffusion length in the order of
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19 300 nm. *D* was observed to increase with the MoS₂ thickness. This strong dependence may be
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21 attributed to weaker in-plane electron-phonon interaction for thicker samples, their enhanced
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23 screening of long-range disorder, and improved charge impurities mitigation. No electric field or
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25 electrical contacts applied on the sample during this technique assures that the results could
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27 reflect the intrinsic properties of 2D materials. *R* is determined as 1.22~1.87×10⁻⁷ K·m²/W,
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29 decreasing with the MoS₂ thickness. This could be caused by the reduced interface spacing
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31 increase under laser heating for thicker samples, and the increased stiffness of thicker samples.
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33 The local interface spacing was uncovered by comparing the theoretical Raman intensity and
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35 experimental data, and was correlated with the observed *R* variation. To our best knowledge, ET-
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37 Raman could also be used for carrier transport and interface energy coupling study of other 2D
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39 materials in the most applicable forms with high accuracy and confidence. Such an impactful
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41 state-resolved technique opens up a new way for efficient and accurate 2D materials thermal and
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43 electrical properties characterization.
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52 53 **Materials and Methods**

54 55 **MoS₂ nanosheets sample preparation**

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3 Seven few-layered MoS₂ samples are prepared by the most widely-used micromechanical
4 cleavage technique from their parent bulk MoS₂ crystals (429MS-AB, molybdenum disulfide,
5 small crystals from the USA, SPI Suppliers). Instead of using chemical vapor deposition or
6 liquid exfoliation, we use mechanical exfoliation because it could efficiently produce clean, high
7 quality atomically thin layered structures for their pristine properties and ultimate device
8 performance studies.⁶⁴ As in the typical micromechanical exfoliation process, an ordinary
9 adhesive Scotch tape and gel film (Gel-Film, PF-20/1.5-X4, Gel-Pak) are used to prepare layered
10 MoS₂ nanosheets on a freshly cleaned c-Si substrate [*p*-doped, (100)-oriented, 0-100 Ω·cm
11 resistivity, ~335 μm thickness] from University Wafer Company (Boston, MA).^{11, 65} The lateral
12 size of layered MoS₂ nanosheets has an equivalent radius ranging from 2.5 to 6.2 μm. We use an
13 optical microscope, atomic force microscope (AFM) (Model MMAFM-2, Digital Instruments,
14 CA, USA) and Raman spectroscopy to identify and locate the MoS₂ nanosheets.
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32 **Experimental details**

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35 We perform the Raman experiments by using a confocal Raman system that consists of a Raman
36 spectrometer (Voyage™, B&W Tek, Inc.) and a microscope (Olympus BX53). The 532 nm CW
37 laser or ps laser is introduced to the Raman system and the laser power is adjusted by a
38 motorized neutral-density (ND) filter system (CONEX-NSR1 and NSND-5, Newport
39 Corporation). The laser source could be switched by the flip mounted mirror before it enters the
40 Raman system without any other change in the experiment setup. To search for and identify the
41 MoS₂ sample under the microscope, we use a 3D piezo-actuated nano-stage (MAX313D,
42 Thorlabs, Inc.) which has a resolution of ~5 nm. This stage is also used in the following Raman
43 shift scanning experiment and it provides us accurate step size. The laser beam is focused on a
44 specific area of the samples (as shown in Fig.3).
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3 During the experiments, we use LabVIEW-based software to fully control the Raman
4 spectrometer, the motorized ND filter, and 3D nano-stage. The Raman spectrometer could
5 automatically acquire and store the spectrum for each energy level after the ND filter is set or
6 each position after the 3D nano-stage is set during the scanning Raman experiment. This
7 significantly shortens the experiment time, reduces the external disturbance, and therefore
8 improves the precision and accuracy of the experiments. By analyzing the Raman spectrum, we
9 could evaluate the RSC of MoS₂ and c-Si. Based on the RSC under different heating states, we
10 can directly determine the hot carrier diffusion coefficient and interfacial thermal resistance.
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23 **3D numerical simulation model**

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26 The 3D numerical modeling is based on the finite volume method, we use this to calculate the
27 temperature rise to determine the hot carrier diffusion coefficient (D) and the interface thermal
28 resistance (R). As shown in Figure. 6(a), the computational domain of the substrate has a radius
29 and thickness of 50 μm . The MoS₂ sample is with the actual size and thickness as those in the
30 experiment. The smallest mesh size along the thickness direction is 0.1 nm with an increasing
31 ratio of 1.02 from the MoS₂ surface to the substrate. The smallest mesh size is 1 nm in the radial
32 direction with the same increasing ratio (1.02). In the modeling, the thermal conductivity of
33 MoS₂ in the in-plane and cross-plane directions is taken as $k_{\square} = 52 \text{ W/m}\cdot\text{K}$ ⁶⁶ and $k_{\perp} = 2$
34 $\text{W/m}\cdot\text{K}$ ⁶⁷, respectively. $k_{\text{c-Si}} = 148 \text{ W/m}\cdot\text{K}$ is for c-Si.⁶⁸ $P = 1 \text{ mW}$ is the excitation laser energy
35 before entering the sample for both CW laser and ps laser sources and the laser spot size is
36 identical to the experiment. For the in-plane thermal conductivity of MoS₂, we also perform the
37 sensitivity study of D and R to it. This could be found in the Supporting Information S6. As
38 considered in our previous work, the MoS₂ nanosheets have the thickness dependent bandgap.²⁷
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3 The E_g values for our seven MoS₂ samples are extracted as summarized in Table S1. This
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5 consideration, instead of using a constant E_g value, could help us determine R and D values with
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7 greater confidence. After the model setup, the carrier diffusion equation [Eq. (1)] is solved and
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9 then the heat conduction one with the hot carrier concentration $\Delta N(r, t)$ used in the source term.
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21 **Notes**

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24 The authors declare no competing financial interest.

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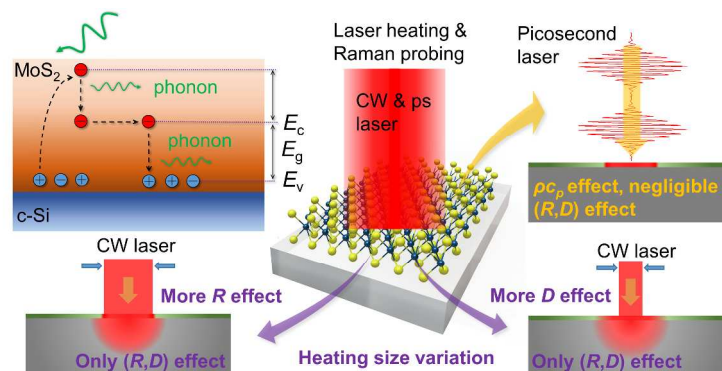
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41 **ASSOCIATED CONTENT**

42
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44 **Supporting Information**

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46 Physical model details for picosecond Raman, data reduction details, ET-Raman experiment
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48 results summary, laser pulse accumulation effect from substrate, the effect of optical properties,
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50 Sensitivity of D and R to MoS₂ in-plane thermal conductivity, and the interference induced
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52 Raman enhancement.
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